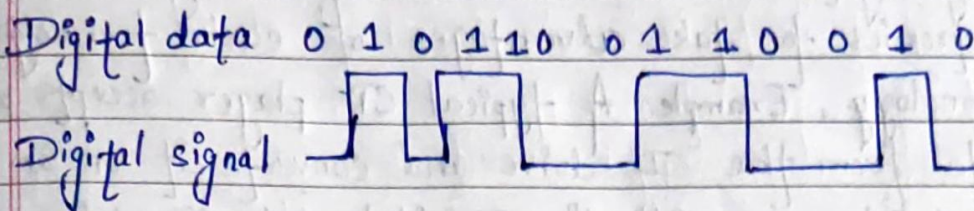


20ECT-115

Digital Signal RepresentationWhat is Digital Electronics

- Digital electronics deals with the electronic manipulation of numbers, or with the manipulation of varying quantities by means of numbers. Because it is convenient to do so, today's digital systems deal only with the numbers 'zero' and 'one', because they can be represented easily by 'off' and 'on' within a circuit.
- Digital stand for digit, digital electronics basically has two conditions which are possible, 0 (low logic) and 1 (high logic).
- Digital electronic systems use a digital signal that are composed of mathematical features to work.
- "1" as true and "0" as false are called bit and the group of bits are named byte.
- Digital electronic circuits are usually made from large assemblies of logic gates.
- Digital ~~describes~~ describes electronic technology that generates, stores, and processes data in terms of two states: 1 and ~~not~~ number 0.

Analog Vs Digital

Many systems use a maximum of analog and digital electronics to take advantages of each technology. Example: A typical CD player accepts digital data from the CD drive and converts it on an analog signal for amplification. Digital data CD drive
10110011101 Analog reproduction of music audio
signal Speaker Sound waves Digital-to-analog converter
Linear amplifiers.

Analog Signal Vs Digital Signal Representation

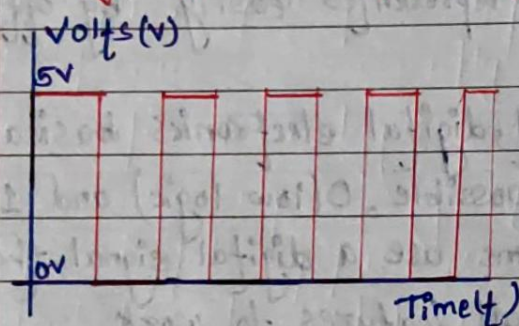


Fig:- Digital signal comprises of only two values High by 1 bit (5V) & Low by 0 bit (0V)

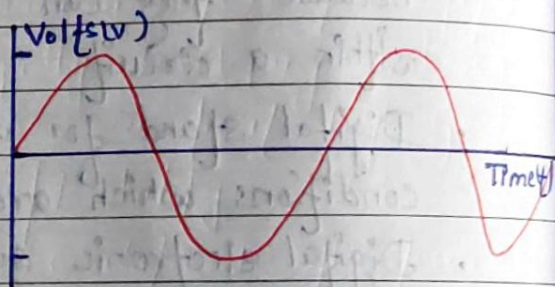
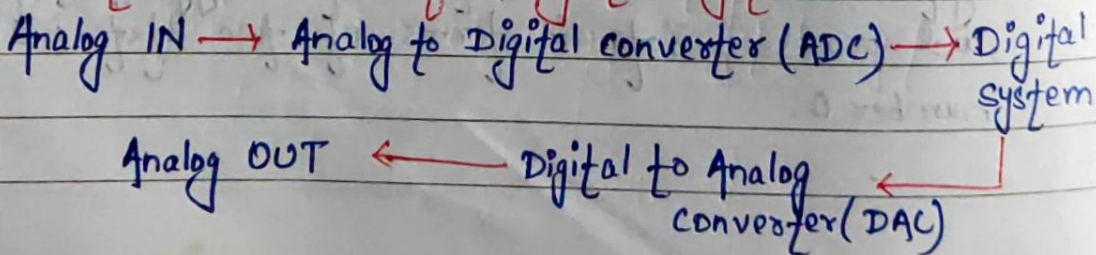


Fig:- Analog signal comprises of infinite values between given limits

How the conversion of Analog to Digital occurs?



Benefits of Digital over Analog

- Reproducibility
- Not effected by noise means quality
- Ease of design
- Data protection Programmable Speed
- Economy

Advantages of Digital Electronics

- Computer-controlled digital systems can be controlled by software, allowing new functions to be added without changing hardware.
- Information storage can be easier in digital systems than in analog ones.
- The noise-immunity of digital systems permits data to be stored and retrieved without noise.
- In a digital system are easier to design and more precise representation of a signal can be obtained by using more binary digits to represent it.
- More digital circuitry can be fabricated on IC chips.
- Error management method can be inserted into the signal path. To detect errors, and then either correct the errors, or at least ask for a new copy of the data.

Disadvantages of Digital Electronics

- Digital circuits are sometimes more expensive, especially in

small quantities.

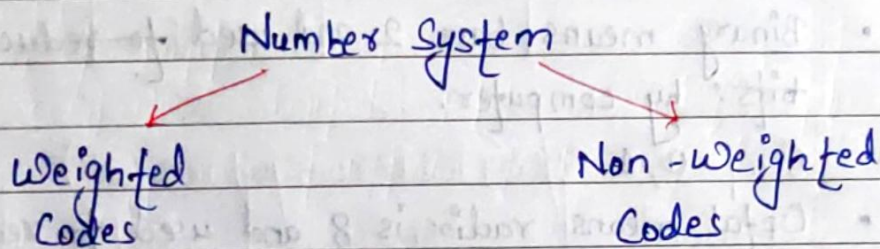
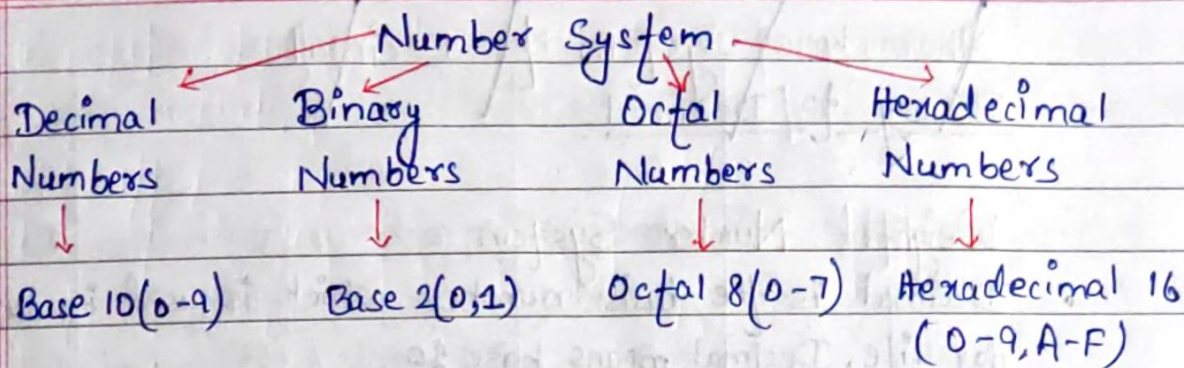
- Conversion to digital format and re-conversion to analog format is needed, which always include the loss of information.
- In some cases, digital circuits uses more energy than analog circuits and produce more heat and need heat sinks.

Applications of Digital Electronics

It's applications are infinite, ranging from high end computing to miniature circuits that can be very versatile, signal processing, communication etc. Digital Electronics is currently rapidly developing and removing conventional analogue machines due to its high speed, more accuracy and greater flexibility.

- The digital systems send the data in the form of packets of digital codes, thus we can encode and decode them in various formats and codes.
 - Data encryption is also possible in the digital systems hence the data transmission is more secure, and can be manipulated in many formats.
 - Digital systems are much advantageous in communications.
- ### Data Transmission using Digital Systems.

2DECT-115



Number System

A number system is the set of certain set of values used to represent any physical quantity. For example: UID of student, number plate of car, $(2A)_{16}$ and $(52)_8$ and $(42)_{10}$

Radix or Base :- Each number set is defined with particular digits or bits

Types of Number Systems

- Decimal
- Binary
- Octal
- Hexadecimal
- BCD
- Excess - 3
- Gray Code

Other Base System to Decimal

Binary to Decimal

Weighted Number System

- Decimal is the basis number which is used in our day to day life. Decimal means base 10
0, 1, 2, 3, 4, 5, 6, 7, 8, 9
- Binary means base 2 and used to reduce the number bits by computer.
0, 1
- Octal means radix is 8 and used to reduce the number bits.
0, 1, 2, 3, 4, 5, 6, 7
- Hexadecimal means base is 16 used in assembly language
0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F
- Base 5 means 5 digits are used.
0, 1, 2, 3, 4
- BCD based on which code is used
i.e., 8421, 2421, 5311

Decimal to Other Base System

Following rules are used

- Divide and multiply by the decimal number to be converted by the base of the desired number system.
- The number before decimal point is to be divided by base

of desired number system and the number after decimal point is to be multiplied by base of the desired number system.

- While dividing the remainder is to be written from Bottom to Top and while multiplying the answer is to be written from Top to Bottom.

Decimal to Binary

$$\begin{array}{r|l} 2 & 29 \\ \hline 2 & 14 \quad 1 \\ 2 & 7 \quad 0 \\ 2 & 3 \quad 1 \\ 2 & 1 \quad 1 \\ & 0 \quad 1 \end{array}$$

$29_{10} = 11101_{2}$ binary

Decimal to Octal

Convert $(73.04375)_{10}$ into octal

$$\begin{array}{r|l} 8 & 73 \quad 1 \\ 8 & 9 \quad 1 \\ & 1 \end{array}$$

$$(73)_{10} = 111_8$$

$$0.4375 \times 8 = 3.5$$

$$0.5 \times 8 = 4.0$$

$$0.4375_{10} = 0.34_8$$

$$(73.04375)_{10} = (1.11.34)_8$$

Decimal to Hexadecimal

Convert $(250.4375)_{10}$ to hexadecimal

$$\begin{array}{r|l} 16 & 250 \\ \hline & 15 \quad A \end{array}$$

$$(250)_{10} = (FA)_{16}$$

$$0.4375 \times 16 = 7.0$$

$$(250.4375)_{10} = FA(FA.7)_{16}$$

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Summary of Various Number Systems

Number system	Radix or base	symbols used	example	application
Decimal	10	0, 1, 2, ..., 9	$(234.9)_{10}$	used by humans
Binary	2	0, 1	$(1001.01)_2$	used in computers
Octal	8	0, 1, 2, 3, ..., 7	$(23.45)_8$	used in computers
Hexadecimal	16	0, 1, 2, ..., 9, A, B, ..., F	$(A57.9F)_{16}$	used in computers

Comparison of Number Systems (2^n)

Decimal	Binary	Octal	Hexadecimal
0	0	0	0
1	1	1	1
2	10	2	2
3	11	3	3
4	100	4	4
5	101	5	5
6	110	6	6
7	111	7	7
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	B
12	1100	14	C
13	1101	15	D
14	1110	16	E
15	1111	17	F

$2^n :- n=1$

$2^1 = 2$

$0 \rightarrow 0$

$1 \rightarrow 1$

$n=2$

$2^2 = 4$

A B

$0 \ 0 = 0$

$0 \ 1 = 1$

$1 \ 0 = 2$

$1 \ 1 = 3$

$n=3$

$2^3 = 8$

A B C

$0 \ 0 \ 0 = 0$

$0 \ 0 \ 1 = 1$

$0 \ 1 \ 0 = 2$

$0 \ 1 \ 1 = 3$

$1 \ 0 \ 0 = 4$

$1 \ 0 \ 1 = 5$

$1 \ 1 \ 0 = 6$

$1 \ 1 \ 1 = 7$

$n=4$

$2^4 = 16$

A B C D

$0 \ 0$

$0 \ 0$

$0 \ 1$

$0 \ 1$

$1 \ 0$

$1 \ 0$

$1 \ 1$

$1 \ 1$

$0 \ 0$

$0 \ 0$

$0 \ 1$

$0 \ 1$

$1 \ 0$

$1 \ 0$

$1 \ 1$

$1 \ 1$

A B C D

$0 \ 0 \ 0 \ 0 = 0$

$0 \ 0 \ 0 \ 1 = 1$

$0 \ 0 \ 1 \ 0 = 2$

$0 \ 0 \ 1 \ 1 = 3$

$0 \ 1 \ 0 \ 0 = 4$

$0 \ 1 \ 0 \ 1 = 5$

$0 \ 1 \ 1 \ 0 = 6$

$0 \ 1 \ 1 \ 1 = 7$

$1 \ 0 \ 0 \ 0 = 8$

$1 \ 0 \ 0 \ 1 = 9$

$1 \ 0 \ 1 \ 0 = A$

$1 \ 0 \ 1 \ 1 = B$

A B C D

$1 \ 1 \ 0 \ 0 = C$

$1 \ 1 \ 0 \ 1 = D$

$1 \ 1 \ 1 \ 0 = E$

$1 \ 1 \ 1 \ 1 = F$

Binary - Hexadecimal

In binary to hexadecimal conversion, 4 binary bits are combined to make one hexa digit based on 8421 code.

$\overset{D}{\curvearrowright}$ $\overset{F}{\curvearrowright}$ $\overset{7}{\curvearrowright}$ $\overset{\text{0000 1010}}{\curvearrowright}$
 1101 1111 0111 . 0000 1010
 $\overset{0}{\curvearrowleft}$ $\overset{A}{\curvearrowleft}$

~~DF7~~ DF7.0A

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Binary to Decimal

$$\bullet (10101.101)_2 \rightarrow ()_{10}$$

$$2^4 \times 1 + 2^3 \times 0 + 2^2 \times 1 + 2^1 \times 0 + 2^0 \times 1 = 16 + 0 + 4 + 0 + 1$$

$$= 21$$

$$2^{-1} \times 1 + 2^{-2} \times 0 + 2^{-3} \times 1 = \frac{1}{2} + 0 + \frac{1}{8} = \frac{4+1}{8} = \frac{5}{8} = 0.625$$

$$(10101.101)_2 \rightarrow (21.625)_{10}$$

Octal to Decimal

$$\bullet (37.6)_8 \rightarrow ()_{10}$$

$$8^1 \times 3 + 8^0 \times 7 = 24 + 7$$

$$= 31$$

$$8^{-1} \times 6 = \frac{1}{8} \times 6 = \frac{3}{4}$$

$$= 0.75$$

$$(37.6)_8 \rightarrow (31.75)_{10}$$

Hexadecimal to Decimal

$$(AC9.B1)_{16} \rightarrow ()_{10}$$

$$16^2 \times 10 + 16^1 \times 12 + 16^0 \times 9 = 2560 + 192 + 9$$

$$= 2761$$

$$16^{-1} \times 11 + 16^{-2} \times 1 = 0.6875 + 0.00390625$$

$$= 0.69140625$$

$$(AC9.B1)_{16} \rightarrow (2761.69140625)_{10}$$

Binary to Octal

$$(10101100.10110)_2 \rightarrow ()_8 \quad 2^3 = 8$$

$$\frac{001}{1} \frac{010}{2} \frac{110}{6} \cdot \frac{101}{5} \frac{100}{4} \Rightarrow (126.54)_8$$

$$(10101101.101011)_2 \rightarrow ()_8$$

$$\begin{array}{cccccc} \underline{010} & \underline{101} & \underline{101} & \underline{101} & \underline{011} & \\ 2 & 5 & 5 & 5 & 9 & \end{array} \Rightarrow (355.54)_8$$

Binary - hexadecimal

$$(101101.101110)_2 \rightarrow ()_{16}$$

$$\begin{array}{cccc} \underline{0010} & \underline{1101} & \underline{1011} & \underline{1000} \\ 2 & D & B & 8 \end{array} \Rightarrow (2D.B8)_{16}$$

$$(10101101.1011010)_2 \rightarrow ()_{16}$$

$$\begin{array}{cccc} \underline{1010} & \underline{1101} & \underline{1011} & \underline{0100} \\ A & D & B & 4 \end{array} \Rightarrow (AD.B4)_{16}$$

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Octal to Binary

$$\begin{aligned} & \cdot (743.26)_8 \rightarrow (\quad)_2 \\ & (111100011.010110)_2 \end{aligned}$$

Hexadecimal to Binary

$$\begin{aligned} & \cdot (AC6.F89)_{16} \rightarrow (\quad)_2 \\ & (101011000110.111110111001)_2 \end{aligned}$$

Binary Arithmetics

Binary
MultiplicationBinary
AdditionBinary
Subtraction

Binary Multiplication

$$\begin{array}{r} \cdot \quad 1111 \\ \quad 1111 \\ \hline \quad 1111 \\ 1111 \times \\ 1111 \times \times \\ 1111 \times \times \times \\ \hline 11100001 \end{array}$$

$$\begin{array}{r} \cdot (1101)_2 \rightarrow (13) \\ \quad (1001)_2 \rightarrow (9) \\ \hline \quad 1101 \\ \quad 0000 \times \\ \quad 0000 \times \times \\ \quad 1101 \times \times \times \\ \hline 1110101 \end{array}$$

Binary Addition

$$\begin{array}{r} 101110.101011 \\ 110111.011110 \\ \hline 1100110.001001 \end{array}$$

Octal addition

$$\begin{array}{r} (742.63)_8 \\ (623.54)_8 \\ \hline 1566.37 \end{array}$$

$$\begin{array}{r} 8 \overline{) 11} \\ \underline{8} \\ 03 \end{array}$$

$$\begin{array}{r} 8 \overline{) 13} \\ \underline{8} \\ 05 \end{array}$$

Binary Subtraction

$$\begin{array}{r} 11011 \\ 10101 \\ \hline 00110 \end{array}$$

$$\begin{array}{r} 01100010 \\ \underline{10101101} \\ 01001101 \end{array}$$

$$\begin{array}{r} 01000010 \\ 10101101 \\ \hline 110010101 \end{array}$$

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Binary Subtraction

12	8	6	4	3	2	1	6	8	4	2	1
1	0	0	0				0	1	0	0	0
-	0	0	1	1			1	0	1	0	1
0	1	0	1				-	0	1	1	0

1's and 2's complement / Sign Magnitude Representation

+5 101

-5 101

0 represent +ve sign

1 represent -ve sign

Unsigned	Signed	1's complement	2's complement
+5 101	0101	0101	0101
-5 -	1101	1010	1011

1's Complement Procedure

$$0110 \rightarrow 1001 \quad (0 \rightarrow 1, 1 \rightarrow 0)$$

4

2's Complement Procedure

$$0110 \rightarrow 1001$$

1

$$\underline{1010}$$

• +123

64 32 16 8 4 2 1

0 1 1 0 1 1

-123

1 0 0 0 0 1 0 0 → 1's complement

1 0 0 0 0 1 0 1 → 2's complement

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1's Complement Arithmetic

$$\text{Range} :- (2^{n-1}-1) \text{ to } +(2^{n-1}-1)$$

Case I

$$\bullet \quad +5 - 4$$

$$+5 + (-4)$$

~~5~~

$$+5 = 0101$$

$$+4 = 0100$$

$$-4 = 1011$$

$$0101$$

$$1011$$

$$\textcircled{1}0000 \Rightarrow 0000$$

$$\begin{array}{r} 1 \\ 0001 \end{array} \Rightarrow + (001) = +1 \text{ Ans}$$

$$\bullet \quad +125 - 63$$

$$+125 \Rightarrow \text{64 32 16 8 4 2 1}$$

$$0 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$$

$$+63 = 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1$$

$$-63 = 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0$$

$$+125 = 0 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$$

$$10 \ 0 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$$

$$1$$

$$00111110 = + (0111110) \text{ Ans}$$

Case II

$$\bullet \quad +2 - 6$$

$$+2 + (-6)$$

$+2 = 0010$

$+6 = 0110$

 -6

$-6 = 1001$

$$\begin{array}{r} 0010 \\ 1001 \\ \hline 1011 \end{array} = -(100) \text{ Ans}$$

-4

Case III

$-5 - 2$

$-5 + (-2)$

$+5 = 0101$

$+2 = 0010$

$-5 = 1010$

$-2 = 1101$

$$\begin{array}{r} 1010 \\ 1101 \\ \hline 0111 \\ 1 \\ \hline 1000 \end{array} = -(111) = -7 \text{ Ans}$$

Case IV

$-5 - 4 = -9$

$-5 + (-4)$

$+5 = 00101$

$+4 = 00100$

$-5 = 11010$

$-4 = 11011$

$$\begin{array}{r} 11010 \\ 11011 \\ \hline 10101 \\ 1 \\ \hline 10110 \end{array} = -(1001) = -9 \text{ Ans}$$

~~-(1001) = -9~~

2's Complement Arithmetic

Range: $-(2^{n-1})$ to $+(2^{n-1}-1)$

Case I

$$\begin{array}{r}
 +5 - 2 \\
 +5 = 0101 \\
 +5 + (-2) \\
 +2 = 0010 \\
 -2 = 1101 \\
 \quad \quad \quad \underline{\quad 1} \\
 \quad \quad \quad 1110
 \end{array}$$

$$\begin{array}{r}
 0101 \\
 1110 \\
 \hline
 0011 = +(011) = +3 \text{ Ans}
 \end{array}$$

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Case II

$$\bullet +2 - 6 \Rightarrow +2 + (-6)$$

$$+2 = 0010$$

$$+6 = 0110$$

$$-6 = 1010$$

$$-6 = 1001$$

$$\begin{array}{r} 1100 \\ \hline \end{array} = -(011)$$

$$\begin{array}{r} 1 \\ \hline 1010 \end{array}$$

$$\begin{array}{r} 1 \\ \hline (100) \end{array} \text{ Ans}$$

Case III

$$\bullet -5 - 2 = -5 + (-2)$$

$$+5 = 0101$$

$$+2 = 0010$$

$$-5 = 1011$$

$$-5 = 1010$$

$$-2 = 1101$$

$$-2 = 1110$$

$$\begin{array}{r} 1 \\ \hline 1011 \end{array}$$

$$\begin{array}{r} 1 \\ \hline 1110 \end{array}$$

$$1001 = -(110)$$

$$\begin{array}{r} 1 \\ \hline (111) \end{array}$$

Case IV:-

$$\bullet -5 - 4$$

$$-5 + (-4)$$

$$5 \text{ bits} = -(2^4) + (2^4 - 1)$$

$$+5 = 00101$$

$$+4 = 00100$$

$$-16 + 15$$

$$-5 = 11010$$

$$-4 = 11011$$

$$\begin{array}{r} 1 \\ \hline 11011 \end{array}$$

$$\begin{array}{r} 1 \\ \hline 11100 \end{array}$$

$$11011$$

$$11100$$

$$10111 = -(1000)$$

$$\begin{array}{r} 1 \\ \hline (1001) \end{array}$$

Boolean Algebra

We need boolean algebra in order to minimize boolean expression



No. of gates required is reduced



More gates can be placed in IC.



Area is increased on IC



Cost is reduced

① NOT GATE

0	1	$0 \rightarrow \bar{A} / A'$
1	0	$1 \rightarrow A$

② $\bar{\bar{A}} \rightarrow A$

$$A=0 \Rightarrow \bar{\bar{0}} = \bar{1} = 0$$

② AND GATE

0	0	0	$A \cdot 0 = 0$
0	1	0	$\bar{A} \cdot 0 = 0$
1	0	0	$A \cdot 1 = A$
1	1	1	$\bar{A} \cdot 1 = \bar{A}$

$$(ii) A \cdot A = A$$

$$A=0 \Rightarrow 0 \cdot 0 = 0$$

$$A=1 \Rightarrow 1 \cdot 1 = 1$$

$$\bar{A} \cdot \bar{A} = \bar{A}$$

$$(iii) A \cdot \bar{A} = 0$$

$$A=0 \Rightarrow 0 \cdot 1 = 0$$

$$A=1 \Rightarrow 1 \cdot 0 = 0$$

③ OR GATE

0	0	0
0	1	1
1	0	1
1	1	1

$$A+0 = A$$

$$A=0 \Rightarrow 0+0 = 0$$

$$A=1 \Rightarrow 1+0 = 1$$

$$(iv) A+A = A$$

$$A=0 \Rightarrow 0+0 = 0$$

$$A=1 \Rightarrow 1+1 = 1$$

$$(v) A+\bar{A} = 1$$

$$A=0 \Rightarrow 0+1 = 1$$

$$A=1 \Rightarrow 1+0 = 1$$

$$(vi) A+1$$

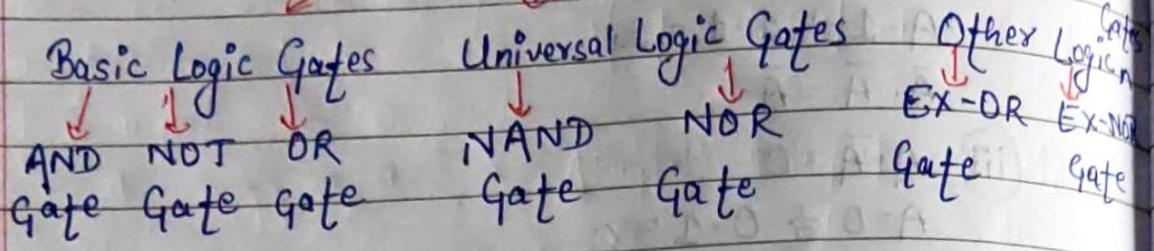
$$A=0 \Rightarrow 0+1 = 1$$

$$A=1 \Rightarrow 1+1 = 1$$

Q $AB + A\bar{B}$ (Minimize this boolean expression using boolean algebra)
 $A(B + \bar{B}) \Rightarrow A \cdot 1 = A$

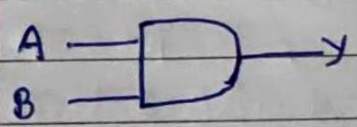
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Logic Gates



AND LOGIC GATE

AND gate has n no. of inputs and one output whereas in the symbol there are only two inputs. IC used for two input AND gate is 7408.

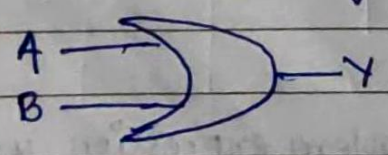


A(input)	B(input)	Y(output)
0	0	0
0	1	0
1	0	0
1	1	1

Boolean Expression: $Y = A \cdot B$

OR LOGIC GATE

OR gate has n no. of inputs and one outputs whereas in the symbol there are only two inputs. IC used for two input OR gate is 7432.



A(input)	B(input)	Y(output)
0	0	0
0	1	1
1	0	1
1	1	1

Boolean Expression: $Y = A + B$

NOT LOGIC GATE

NOT gate has only one input and one output. IC used for two input NOT gate is 7404.

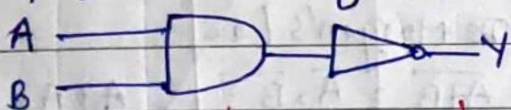


Boolean Expression: $Y = \bar{A}$

A (input)	Y (output)
0	1
1	0

NAND LOGIC GATE

NAND gate has n no. of ~~outputs~~ inputs and one output whereas in the symbol there are only two inputs. IC used for two input NAND gate is 7400.



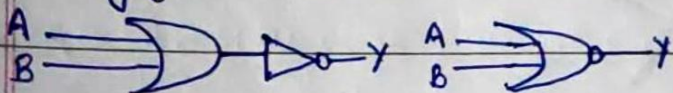
A (input)	B (input)	Y (output)
0	0	1
0	1	1
1	0	1
1	1	0

Boolean expression

$$Y = \overline{A \cdot B} / \bar{A} + \bar{B}$$

NOR LOGIC GATE

NOR gate has n no. of inputs and one output whereas in the ~~symbol~~ symbol there are only two inputs. IC used for two input NOR gate is 7402.

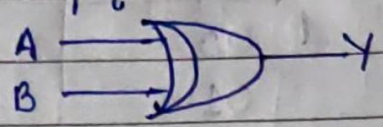


Boolean expression: $Y = \overline{A + B} / \bar{A} \cdot \bar{B}$

A (input)	B (input)	Y (output)
0	0	1
0	1	0
1	0	0
1	1	0

EX-OR LOGIC GATE

XOR gate has n no. of inputs and one outputs whereas in the symbol there are only two inputs. IC used for two input XOR is 7486



A(input)	B(input)	Y(output)
0	0	0
0	1	1
1	0	1
1	1	0

Boolean Expression: $Y = A \oplus B$

Boolean Laws

Commutative Law

$$AB = BA$$

$$A+B = B+A$$

Distributive Law

$$A(B+C) = AB+AC$$

$$A+BC = (A+B)(A+C)$$

Associative Law

$$A(BC) = (AB)C$$

$$A+(B+C) = (A+B)+C$$

De-Morgan's Law

$$\overline{A+B} = \bar{A} \cdot \bar{B}$$

$$\overline{AB} = \bar{A} + \bar{B}$$

$$A+A = A$$

$$A+0 = A$$

$$\bar{A} + A = 1$$

$$A+1 = 1$$

$$A \cdot A = A$$

$$A \cdot 0 = 0$$

$$\bar{A} \cdot A = 0$$

$$A \cdot 1 = A$$

$$0' = 1$$

$$A'' = A$$

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Boolean Expression

$$\text{(vii)} \quad (A+B) \cdot (A+C) = AA+BC = A+BC \quad (\text{Distribution Theorem})$$

$$\text{(viii)} \quad AB + \bar{A}C + B^*C = AB + \bar{A}C \quad (\text{Consensus Theorem})$$

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Date:- 12/9/2020

(ix) Demorgan Law

$$\overline{x+y} = \bar{x} \cdot \bar{y}$$

$$\overline{\bar{x} \cdot \bar{y}} = \overline{\bar{x}} + \overline{\bar{y}} = x+y$$

Weighted / Non-weighted Codes

1. Grey Code (non-weighted codes) → EXOR GATE

Binary

1 0 1 1 0 1 0

↓
Process

Grey

1 1 1 0 1 1 1

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Date:- 14/9/2020

• Grey

1 0 1 1 0 1 0

↓
Process

Binary

1 1 0 1 1 0 0

2. Binary Coded Decimal (BCD code) / 8421 code (weighted code)

BCD (limited weighted)

Binary (weight not limited)

8 4 2 1

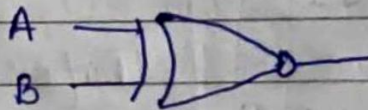
... 128 64 32 16 8 4 2 1

0-9 (same as binary)

	8	4	2	1	
0	0	0	0	0	$10 \rightarrow 00010000$
1	0	0	0	1	$226 \rightarrow 00100010010110$
2	0	0	1	0	$19672 \rightarrow 00011001011001110010$
3	0	0	1	1	110010
4	0	1	0	0	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	

Boolean Algebra + Gates

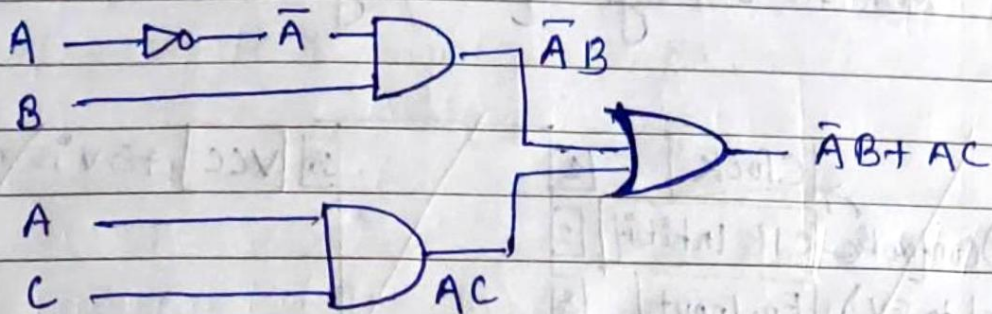
EXNOR LOGIC Gate



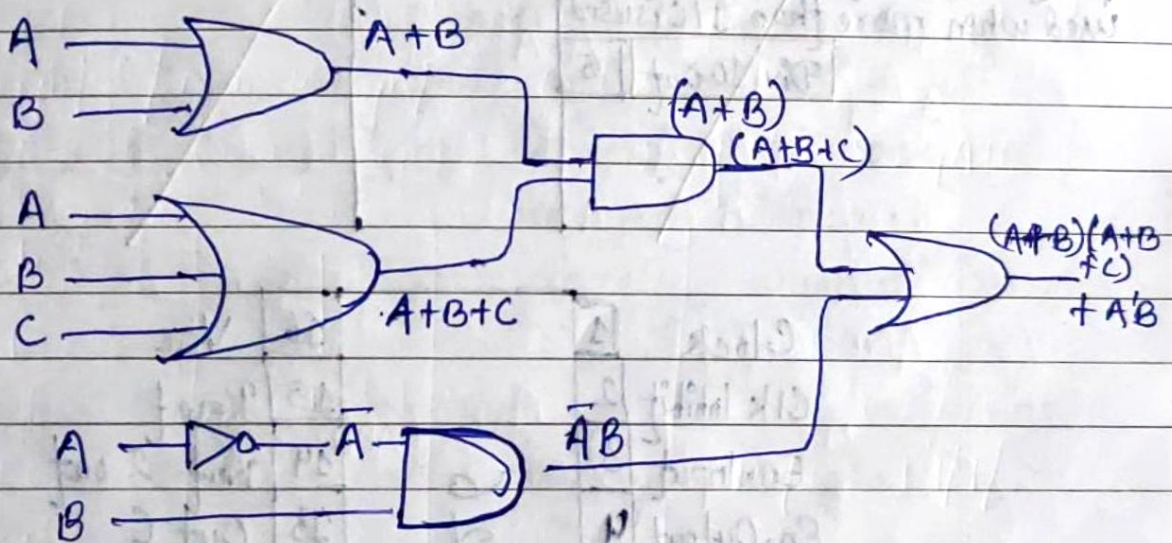
$$\overline{A \oplus B}$$

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

eg:- $\bar{A}B + AC$ Implement it using gates



$y = (A+B)(A+B+C) + A'B$ Using Gate



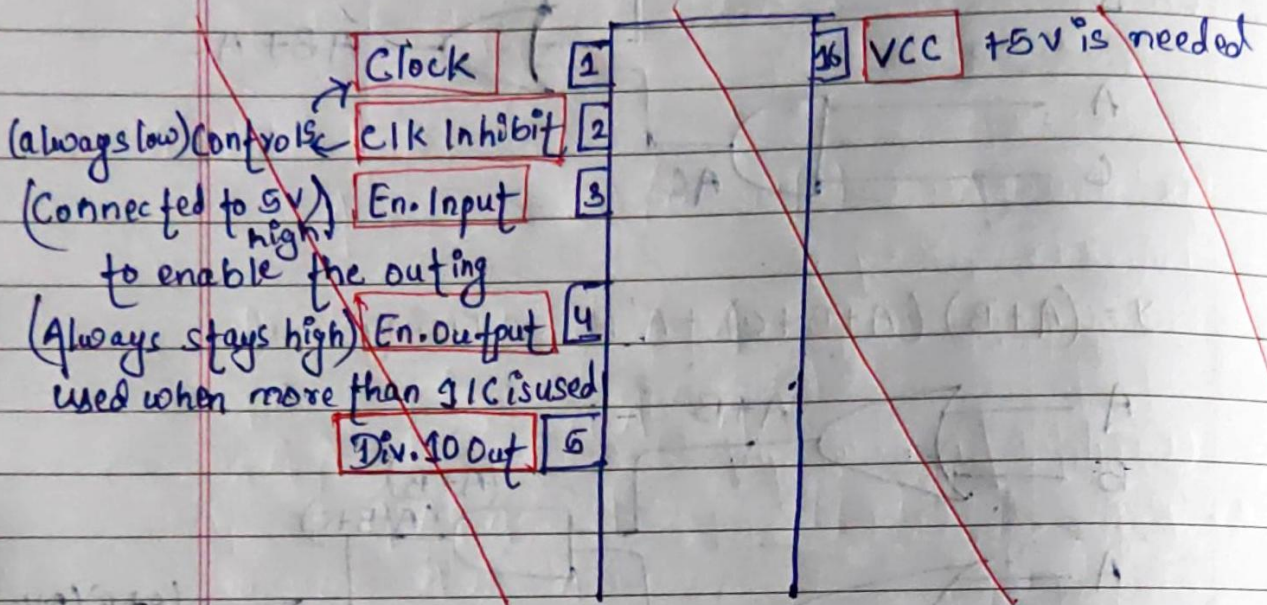
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CD4026G - An IC that performs a function of both a counter as well as seven segment drivers.

Dark $\rightarrow R \uparrow, C \downarrow, V \uparrow$ ($V = IR$)

Light $\rightarrow R \downarrow, C \uparrow, V \downarrow$

- when the clock goes low to high, 0-9 ~~dispt~~ count will on 7 segment display.



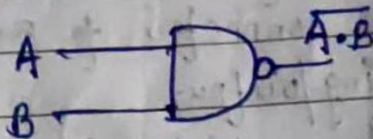
Clock	1	16	Vcc
CLK Inhibit	2	15	Reset
En. Input	3	14	Not 2 out
En. Output	4	13	Out C
Div. 10 out	5	12	Out B
Out F	6	11	Out E
Out G	7	10	Out A
Gnd	8	9	Out D

CD4026

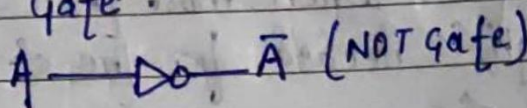
- Clock - when it changes from ~~high~~ low to high, 0-9 count occurs on 7 segment display.

- Clk inhibit - It is always low due to which clock works. It controls clock.
- En. Input - It is connected to 5V (high) to enable the output/output.
- En. Output - Always high. It is needed when to cascade when more than 1 IC is used.
- VCC - +5V (high) is needed for the circuit to work.
- Gnd - Ground pin
- Div. 10 out - It gives a pulse when the count 0 to 9 is completed. It is also helpful in cascading other IC with this IC.
- Out F, G, C, B, E, A, D - Output pins connected to 7 segment display.
- Not 2 out - used very rarely when division is needed.
- Reset - Resets the count to 0. (After giving 1 0 is compulsory for this pin).

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Universal GatesNAND GATE

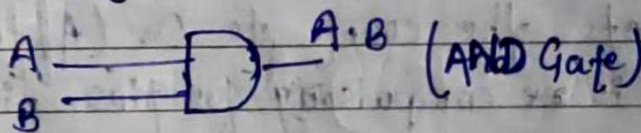
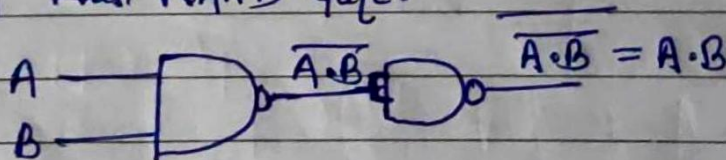
① NOT Gate :-

In NAND Gate if $B = A$ 

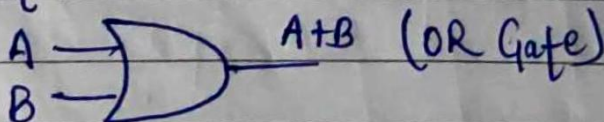
$$A \cdot A = A$$

Therefore $\overline{A \cdot A} = \bar{A}$

② AND Gate :-

In ~~AND~~ NAND Gate.

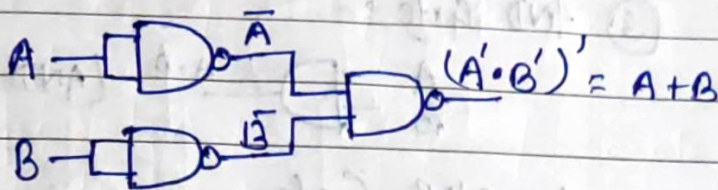
③ OR Gate :-



In NAND Gate

~~AND~~

P

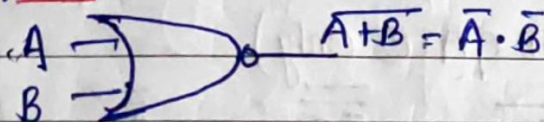


$(A' \cdot B)'$ By applying DeMorgan's theorem

$(A')' + (B)'$

$A + B$

NOR GATE



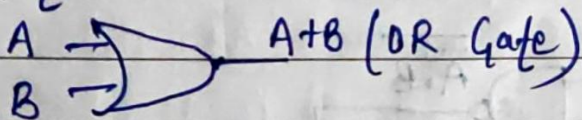
① NOT Gate:-

$A \rightarrow \text{NOT} \rightarrow \bar{A}$ (NOT Gate)

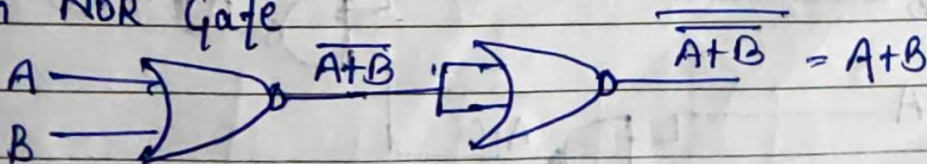
In NOR Gate, if $B = A$



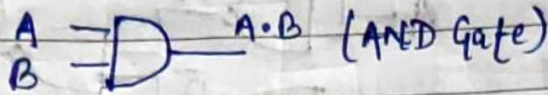
② OR Gate :-



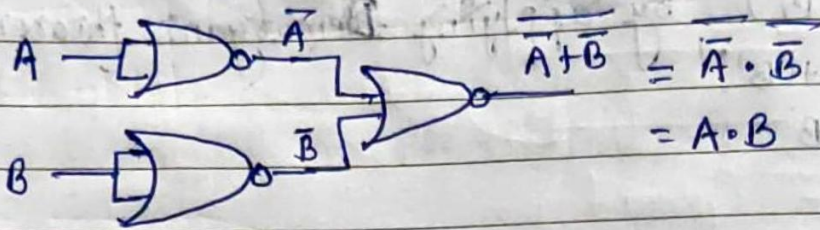
In NOR Gate



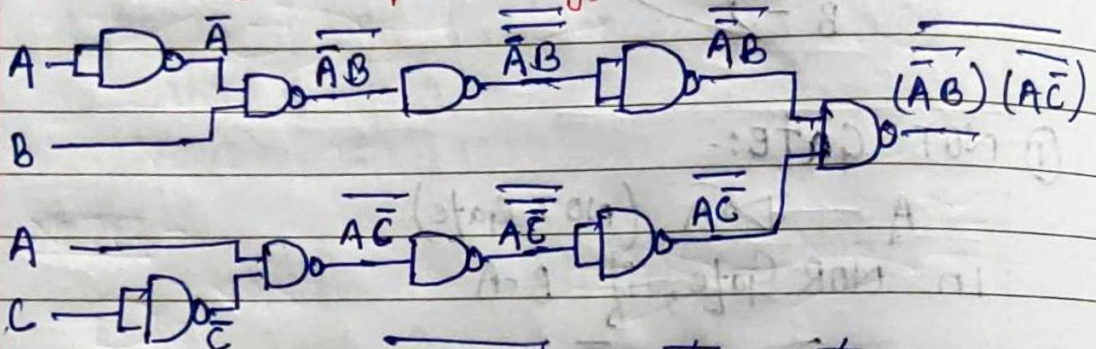
③ AND Gate :-



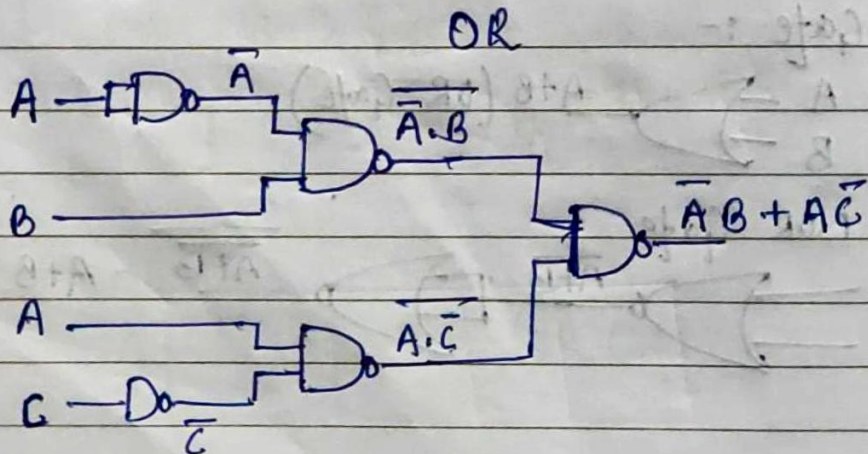
In NOR Gate



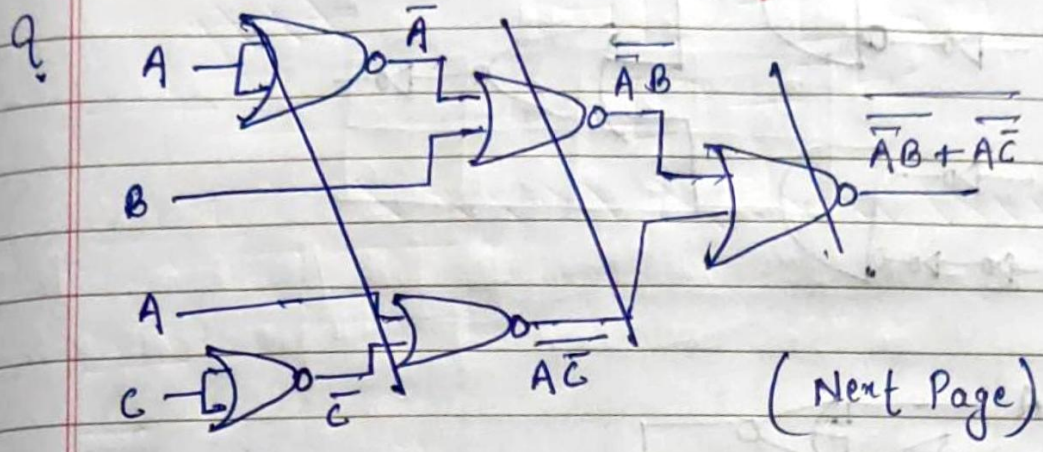
Q $\overline{A}B + A\overline{C}$ (NAND GATE Only)



$$\text{Now, } (\overline{A}B)(A\overline{C}) = \overline{\overline{\overline{A}B} + \overline{A\overline{C}}} = \overline{\overline{A} + \overline{C}} = A'B + AC'$$



Q $\bar{A}B + A\bar{C}$ (NOR GATE only)



K-Map (Karnough Map)

It is the graphical representation of reducing the boolean expression

$2^n, n=2, 2^n=4$

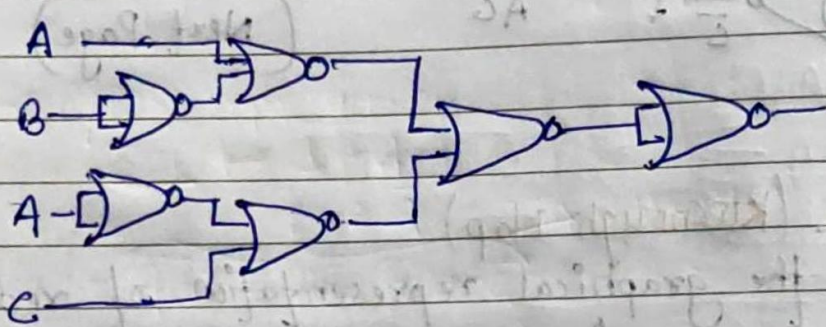
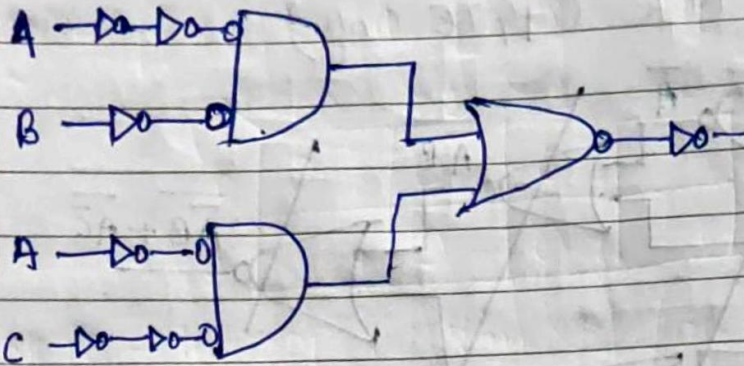
	A B	0	1	
0		0	1	A, B
1		2	3	

$n=3, 2^n=8$

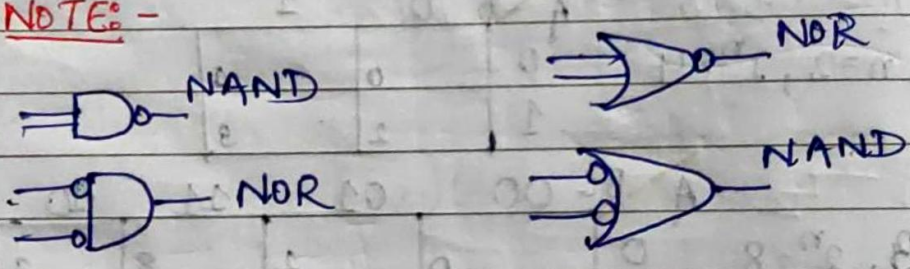
	A BC	00	01	11	10	
0		0	1	3	2	A, B, C
1		4	5	7	6	

$n=4, 2^n=16$

	AB CD	00	01	11	10	
00		0	1	3	2	A, B, C, D
01		4	5	7	6	
11		12	13	15	14	
10		8	9	11	10	



NOTE:-



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A, B

	B	0	1
A	0	0	1
	1	2	3

A, B, C

	BC	00	01	11	10
A	0	0	1	3	2
	1	4	5	7	6

A, B, C, D

	CD	00	01	11	10
A	00	0	1	3	2
	01	4	5	7	6
	11	12	13	15	14
	10	8	9	11	10

SOP/POS (Sum of products/Product of sums)

- $\Sigma m \rightarrow$ SOP
↳ min term
- $\Pi M \rightarrow$ POS
↳ max term

eg 1: - $f(A, B) = \Sigma m(0, 1, 3)$ Reduce minimized boolean exp. using K-map

	B	0	1
A	0	1	1
	1	2	3

$$\text{eg 2: } f(A, B, C) = \prod_m [0, 1, 3, 5, 7]$$

	BC	00	01	11	10
A	0	0	0	0	2
	1	4	0	0	6

NOTE:- In SOP we have to fill the boxes with 1 &
In POS we have to fill the boxes with 0

SOP/POS expressions:-

$$\text{SOP} \rightarrow 1 \rightarrow A$$

$$0 \rightarrow \bar{A}$$

→ Canonical form

$$\text{eg 3: } \bar{A}\bar{B}C + A\bar{B}C + ABC$$

$$(001) \quad (101) \quad (110)$$

1

5

6

$$\rightarrow f(A, B, C) = \sum_m (1, 5, 6)$$

↙ standard form

$$\text{POS} \rightarrow 1 \rightarrow \bar{A}$$

$$0 \rightarrow A$$

$$\text{eg 4: } (A + \bar{B} + C) (\bar{A} + \bar{B} + \bar{C}) (A + \bar{B} + \bar{C})$$

$$(010) \quad (111) \quad (011)$$

2

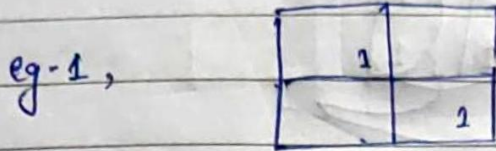
7

3

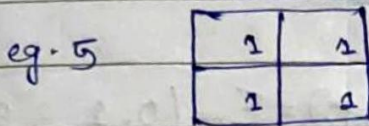
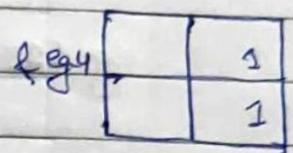
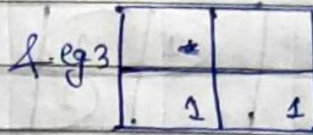
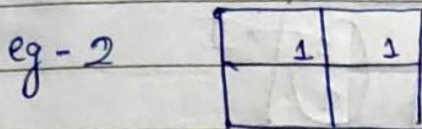
	BC	00	01	11	10
A	0	0	1	0	2
	1	4	5	0	6

Grouping

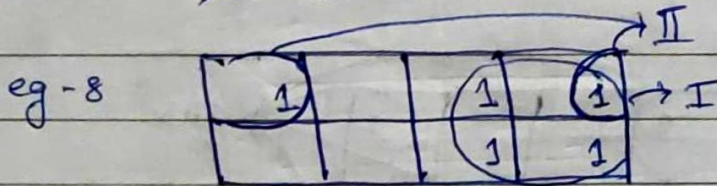
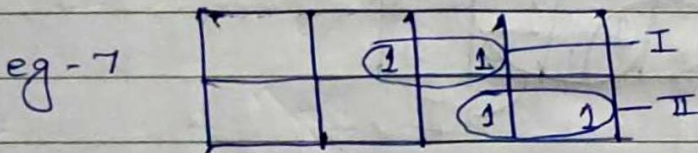
2, 4, 8, 16 → Priority := 16
8
4
2

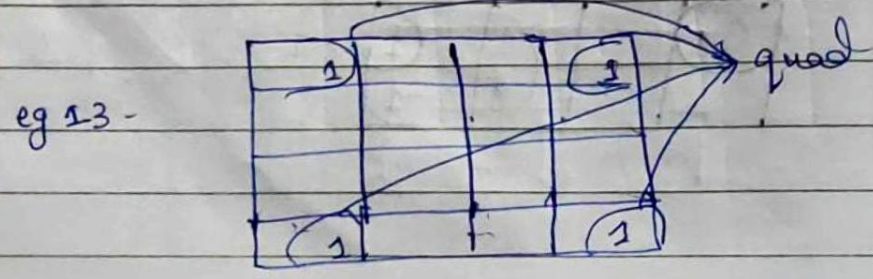
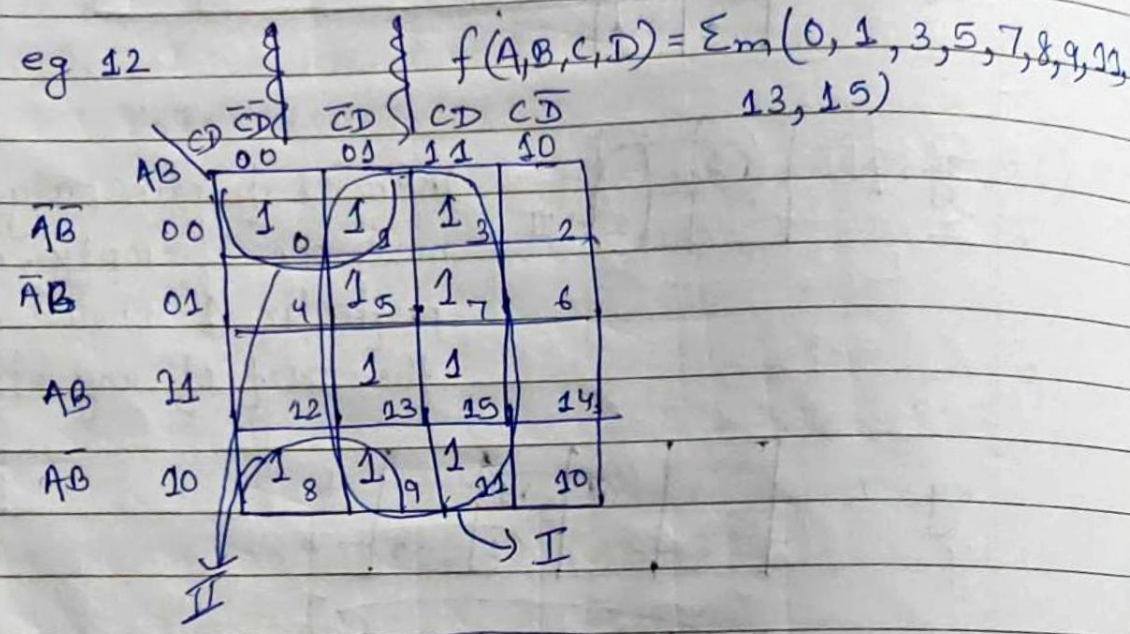
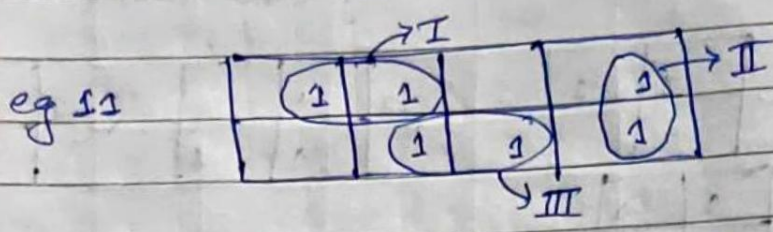
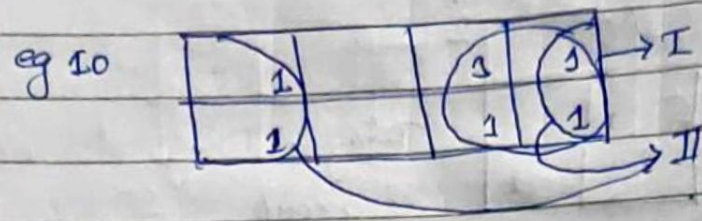
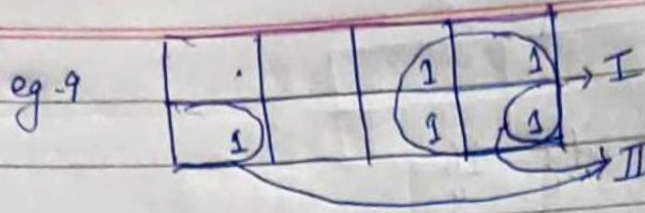


Diagonal Diagonals never make a group



In order to make a group I need one 1 empty, means that particular 1 should not be the part of any other group.





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eg 1 :- $f(A, B) = \sum m(2, 3)$

		\bar{B}	B
\bar{A}	0	0	1
A	1	1	1

A	B
1	0
1	1
A	

$$f(A, B) = A$$

eg 2 :- $f(A, B, C) = \sum m(0, 2, 3, 6, 7)$

		$\bar{B}\bar{C}$	$\bar{B}C$	$B\bar{C}$	BC
\bar{A}	0	1	1	1	1
A	1	1	1	1	1

A	B	C
0	1	1
0	1	0

A	B	C
1	1	1

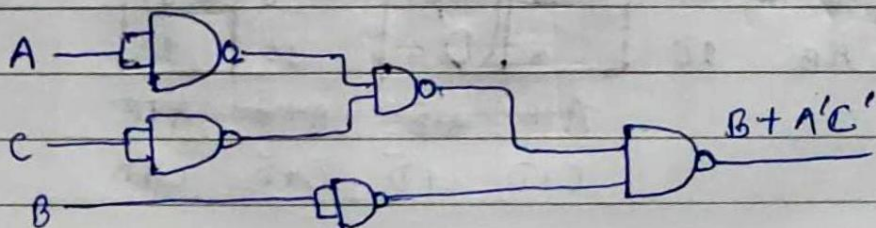
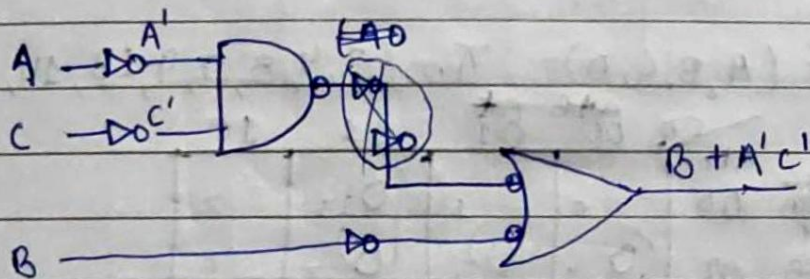
$$f(A, B, C) = B + \bar{A}\bar{C}$$

0	0	0
1	1	0

0	1	0
\bar{A}	\times	\bar{C}

\bar{A}	\times	\bar{C}
-----------	----------	-----------

$B + \bar{A}\bar{C}$ → NAND GATE



eg 3 :- $f(A, B, C, D) = \sum m(0, 1, 3, 5, 7, 8, 9, 11, 13, 15)$

		$\overline{C}D$	$\overline{C}D$	CD	CD
		00	01	11	10
$\overline{A}\overline{B}$	00	1	1	1	2
$\overline{A}B$	01	4	5	7	6
AB	11	12	13	15	14
$A\overline{B}$	10	8	9	11	10

A	B	C	D
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	1	0	1
1	1	1	1
1	0	0	1
1	0	1	1
x	x	x	D

A	B	C	D
0	0	0	0
0	0	0	1
1	0	0	0
1	0	0	1
x	\overline{B}	\overline{C}	x

$f(A, B, C, D) = D + B'C$

eg 4 :- $f(A, B, C, D) = \prod m(3, 4, 5, 7, 9, 13, 14, 15)$

		$\overline{C}D$	$\overline{C}D$	CD	CD
		00	01	11	10
$A+B$	00	0	1	0	2
$A+\overline{B}$	01	0	0	0	6
$\overline{A}+\overline{B}$	11	12	0	0	14
$\overline{A}+B$	10	8	0	1	10

~~$A+B$~~ ~~$A+\overline{B}$~~ ~~$\overline{A}+\overline{B}$~~ ~~$\overline{A}+B$~~
 $C+D$ $C+\overline{D}$ $\overline{C}+D$ $\overline{C}+\overline{D}$

$A \ B \ C \ D$	$A \ B \ C \ D$	$A \ B \ C \ D$	$A \ B \ C \ D$
$0 \ 0 \ 1 \ 1$	$0 \ 1 \ 0 \ 0$	$1 \ 1 \ 0 \ 1$	$1 \ 1 \ 1 \ 1$
$0 \ 1 \ 1 \ 1$	$0 \ 1 \ 0 \ 1$	$1 \ 0 \ 0 \ 1$	$1 \ 1 \ 1 \ 0$
$A \times \bar{C} \bar{D}$	$A \ B \ C \times$	$\bar{A} \times C \bar{D}$	$\bar{A} \bar{B} \bar{C} \times$
$\hookrightarrow A + \bar{C} + \bar{D}$	$\hookrightarrow A + \bar{B} + C$	$\hookrightarrow \bar{A} + C + \bar{D}$	$\hookrightarrow \bar{A} + \bar{B} + \bar{C}$

$$f(A, B, C, D) = (A + \bar{C} + \bar{D}) \cdot (A + \bar{B} + C) \cdot (\bar{A} + C + \bar{D}) \cdot (\bar{A} + \bar{B} + \bar{C})$$

Q7 $f(A, B, C, D) = \sum m(0, 2, 3, 4, 10, 14, 15)$

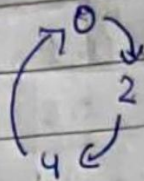
AB	CD	$C+D$ 00	$C+\bar{D}$ 01	$\bar{C}+D$ 11	$C+\bar{D}$ 10	$A \ B \ C \ D$	$A \ B \ C \ D$	$A \ B \ C \ D$
$A \bar{B}$	00	0	1	3	2	0000	0001	1111
$A \bar{B}$	01	4	5	7	6	0001	0011	1110
$A \bar{B}$	11	12	13	15	14	1000	$A+B \times D'$	$\bar{A} + \bar{B} + \bar{C}$
$A \bar{B}$	10	8	9	11	10	1001	$x \ B + C \ x$	

$$f(A, B, C, D) = (B+C) \cdot (A+B+\bar{D}) \cdot (\bar{A} + \bar{B} + \bar{C}) \cdot (\bar{A} + \bar{C} + D)$$

$$\begin{array}{r} \bar{A} \ B \ C \ D \\ 1 \ 1 \ 1 \ 0 \\ \hline \bar{A} \times + \bar{C} + D \end{array}$$

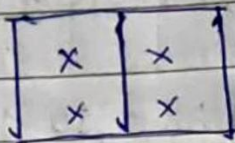
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Don't Care -
Represented by X



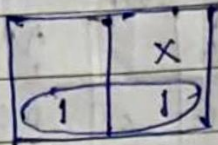
- * In $\Sigma m(SOP) = X \rightarrow 1$
- * In $\Pi m(POS) = X \rightarrow 0$

eg 1:-

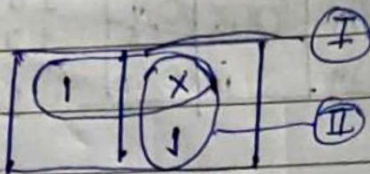


Don't care doesn't group with each other

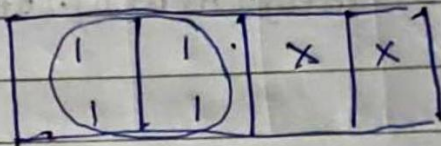
eg 2:-



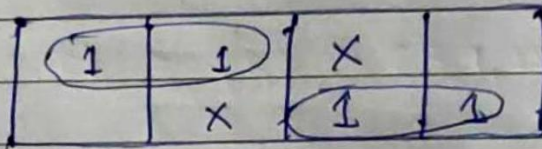
eg 3:-



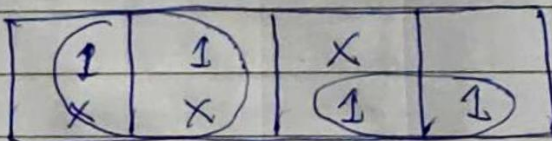
eg 4:-



eg 5:-



eg 6:-



eg 7:- $f(A,B,C,D) = \sum m(0, 1, 3, 5, 7, 8, 9, 11, 13, 15) + \sum d(2, 10)$

AB \ CD	00	01	11	10
00	1	1	1	X
01		1	1	0
11		1	1	0
10	1	1	1	X

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eg 6

	1	2	X	
X	X	X	1	1

A B C D	A B C D
0 0 0 0	1 1 1
0 0 1	1 1 0
1 0 0	AB X
1 0 1	
X B X	

$$\bar{B} + AB = (\bar{B} + B)(\bar{B} + A)$$

$\bar{B} + A = \bar{B} + A$

	$\bar{B}C$	$B\bar{C}$	BC	\bar{C}
\bar{A}	00	01	11	10
A	10	11	X3	2
	X4	X5	17	16

eg 1:-

	BC	00	01	11	10
A	0	0	0	0	2
1		4	5	7	6

eg 2:- $f(A, B, C, D) = \sum m(2, 4, 6, 8, 9, 13) + \sum d(0, 7, 14, 15)$

	CD	$\bar{C}\bar{D}$	$C\bar{D}$	$\bar{C}D$	CD
$\bar{A}\bar{B}$	00	X	1	3	1 2
$\bar{A}B$	01	1 4	5	X 7	1 6
AB	11	X 12	1 13	15	X 14
$A\bar{B}$	10	1 8	1 9	11	10

eg 3:- $f(A, B, C, D) = \sum m(0, 1, 3, 5, 7, 8, 9, 11, 13, 15) + \sum d(2, 10)$

1	0	1	1	1	3	X	2
	4	1	6	1	7		6
	12	1	23	1	15		14
1	8	1	9	1	10	X	10

eg 4:- $\pi_m(1, 2, 4, 6, 8, 10, 14) + \pi_d(0, 3, 8, 12)$

X 0	0 1	X 3	0 2
0 4	5	7	0 6
X 12	13	15	0 14
X 8	0 9	10	0 10

Standard and Canonical form:-

eg:- $AB + BC + AC$

$$AB(C + \bar{C}) + (A + \bar{A})BC + A(B + \bar{B})C$$

$$ABC + AB\bar{C} + ABC + \bar{A}BC + ABC + A\bar{B}C$$

$$ABC + AB\bar{C} + \bar{A}BC + A\bar{B}C \quad \text{--- Canonical form}$$

$$A(B + \bar{B}) + C(\bar{A}B + A\bar{B})$$

$$f(A, B, C) = \sum_m(3, 5, 6, 7) \quad \text{--- Standard form}$$

eg:- $\bar{A} + B$ (min forms)

$$\bar{A}(B + \bar{B}) + (A + \bar{A})B$$

$$\bar{A}B + \bar{A}\bar{B} + AB + \bar{A}B$$

$$\bar{A}B + \bar{A}\bar{B} + AB = \text{min term}$$

$$01 \quad 00 \quad 11$$

$$f(A, B) = \sum_m(0, 1, 3)$$

eg:- $\bar{A}\bar{B}D + AB\bar{C}\bar{D} + ABC\bar{D} + \bar{A}\bar{B}\bar{C}D$ (using universal gate)

$$\bar{A}\bar{B}CD + \bar{A}\bar{B}\bar{C}D + AB\bar{C}\bar{D} + ABC\bar{D} + \bar{A}\bar{B}\bar{C}D$$

$$\bar{A}\bar{B}CD + \bar{A}\bar{B}\bar{C}D + AB\bar{C}\bar{D} + ABC\bar{D}$$

$$0011 \quad 0001 \quad 1100 \quad 1110$$

$$f(A, B, C, D) = \sum_m(3, 1, 12, 14)$$